

Math 115

Fall 2017

Lecture 2



Class Quiz write Your name clearly
Box Your
Final
Answer.

① Evaluate: $5^2 - (-4)^2$

$$= 25 - (16) = 25 - 16 = \boxed{9}$$

② Evaluate $\frac{x-y}{2x}$ for $x=4$ and $y=-4$.

$$= \frac{4 - (-4)}{2(4)} = \frac{4+4}{8} = \frac{8}{8} = \boxed{1}$$

③ Translate: 3 less than twice some number

$$\boxed{2x - 3}$$

Ch. 1

Reduce a Fraction

$$\frac{45}{75} = \frac{\cancel{3} \cdot \cancel{3} \cdot \cancel{5}}{\cancel{3} \cdot \cancel{5} \cdot \cancel{5}} = \frac{3}{5}$$

$$\frac{120}{300} = \frac{12 \cdot \cancel{10}}{30 \cdot \cancel{10}} = \frac{12}{30} = \frac{\cancel{6} \cdot 2}{\cancel{6} \cdot 5} = \frac{2}{5}$$

Simplify

$$\frac{65x^2}{80x} = \frac{\cancel{5} \cdot 13 \cdot \cancel{x} \textcircled{x}}{\cancel{5} \cdot 16 \cdot \textcircled{x}} = \boxed{\frac{13x}{16}}$$

Divide : $\frac{10}{33} \div \frac{25}{77} = \frac{10}{33} \cdot \frac{77}{25}$

$$= \frac{\textcircled{5} \cdot 2}{3 \cdot \cancel{11}} \cdot \frac{7 \cdot \cancel{11}}{\textcircled{5} \cdot 5}$$

$$= \boxed{\frac{14}{15}}$$

Simplify $\frac{12x^2}{25y^3} \div \frac{18x^4}{35y^5} = \frac{\overset{2}{\textcircled{12}x^2}}{\cancel{25}y^3} \cdot \frac{\overset{7}{\cancel{35}y^5}}{\textcircled{18}x^4}$

$$= \boxed{\frac{14y^2}{15x^2}}$$

Simplify $\frac{3}{5} - \frac{-2}{5} = \frac{3 - (-2)}{5}$

$$= \frac{3+2}{5} = \frac{5}{5} = 1$$

Simplify: $\frac{3x+7}{10} + \frac{7x-7}{10} = \frac{3x+7+7x-7}{10}$

$$= \frac{10x}{10} = 1x$$

$$= \boxed{x}$$

Simplify $\frac{2}{3} - \frac{1}{4} = \frac{2 \cdot 4}{3 \cdot 4} - \frac{1 \cdot 3}{4 \cdot 3}$

we must find
LCD

LCD = 12

$$= \frac{8}{12} - \frac{3}{12} = \frac{8-3}{12}$$

$$= \boxed{\frac{5}{12}}$$

Simplify

$$\frac{3}{25} - \frac{7}{10} = \frac{3 \cdot 2}{25 \cdot 2} - \frac{7 \cdot 5}{10 \cdot 5}$$

$25 = 5 \cdot 5$

$10 = 5 \cdot 2$
LCD = $5 \cdot 5 \cdot 2$

LCD = 50

$$= \frac{6}{50} - \frac{35}{50} = \boxed{\frac{-29}{50}}$$

Reduce / Simplify:

$$1) \frac{\overset{2}{\cancel{16}} \overset{5}{x^5}}{\overset{3}{\cancel{24}} x^2} = \boxed{\frac{2x^3}{3}}$$

$$2) \frac{75}{49} \div \frac{-14}{25} = \frac{75}{49} \cdot \frac{-25}{14} = \boxed{\frac{-1875}{686}}$$

$$3) \frac{x-12}{2x+1} + \frac{x+13}{2x+1}$$

$$= \frac{x-12+x+13}{2x+1} = \frac{2x+1}{2x+1} = \boxed{1}$$

$$12 = 2 \cdot 2 \cdot 3$$

$$16 = 2 \cdot 2 \cdot 2 \cdot 2 \Rightarrow \text{LCD} = 48$$

$$4) \frac{5}{12} - \frac{9}{16}$$

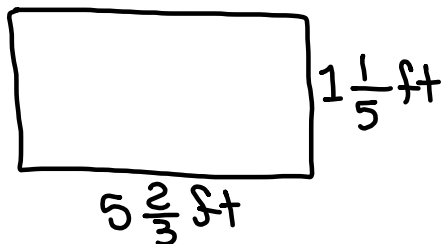
$$= \frac{5 \cdot 4}{12 \cdot 4} - \frac{9 \cdot 3}{16 \cdot 3}$$

$$= \frac{20}{48} - \frac{27}{48}$$

$$= \boxed{\frac{-7}{48}}$$

Find the area

$$\text{Area} = L \cdot W$$



$$5 \overline{) 34} \\ \underline{-30} \\ 4$$

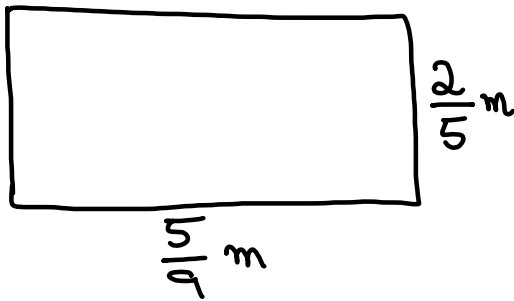
$$A = L \cdot W$$

$$= 5 \frac{2}{3} \cdot 1 \frac{1}{5}$$

$$= \frac{17}{3} \cdot \frac{6}{5}$$

$$= \frac{34}{5} = \boxed{6 \frac{4}{5} \text{ ft}^2}$$

Find the perimeter



$$= 1 \frac{41}{45} \text{ m}$$

$$P = 2L + 2W$$

$$P = 2 \cdot \frac{5}{9} + 2 \cdot \frac{2}{5}$$

$$= \frac{2 \cdot 5}{1 \cdot 9} + \frac{2 \cdot 2}{1 \cdot 5}$$

$$= \frac{10}{9} + \frac{4}{5}$$

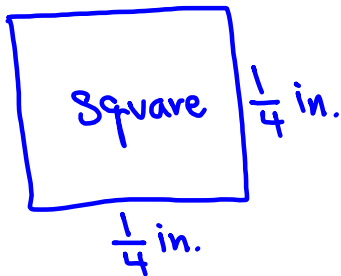
$$\text{LCD} = 45$$

$$= \frac{10 \cdot 5}{9 \cdot 5} + \frac{4 \cdot 9}{5 \cdot 9}$$

$$= \frac{50}{45} + \frac{36}{45} = \frac{86}{45}$$

Find area & Perimeter

$$A = S^2, \quad P = 4S$$



$$A = \left(\frac{1}{4}\right)^2 = \frac{1}{4} \cdot \frac{1}{4}$$

$$= \frac{1}{16} \text{ in}^2$$

$$P = 4\left(\frac{1}{4}\right) = \frac{4}{1} \cdot \frac{1}{4} = \frac{4}{4} = 1 \text{ in}$$

Translate

1) Square of Some number reduced by 8

$$x^2 - 8$$

2) 10 more than Some number cubed.

$$x^3 + 10$$

3) -4 times the difference of 10 and x.

$$-4 \cdot (10 - x)$$

4) Twice the sum of Some number and 6
is equal to 10 less the number

$$2(x + 6) = 10 - x$$

A less B $\rightarrow A - B$

A less than B
 $\rightarrow B - A$

5) when 5 is added to half Some
number, the result is 5 less than
one-third of the number.

$$\frac{1}{2}x + 5 = \frac{1}{3}x - 5$$

Properties of real numbers:

1) Commutative Prop.

$$a + b = b + a$$

$$7 + 3 = 3 + 7$$

$$a \cdot b = b \cdot a$$

$$5 \cdot (-4) = (-4) \cdot 5$$

2) Associative Prop.

$$(a + b) + c = a + (b + c)$$

$$6x + 8 = 8 + 6x$$

$$7(x + 2) = (x + 2) \cdot 7$$

$$a(bc) = (ab)c$$

$$(7 + 2) + 8 = 7 + (2 + 8)$$

$$-8(5x) = (-8 \cdot 5)x$$

$$4(3x) = (4 \cdot 3)x$$

$$(4x + 10) + 8 = 4x + (10 + 8)$$

3) Distributive Prop.

$$a(b + c) = ab + ac$$

$$4(x + 2) = 4x + 4 \cdot 2$$

$$-6(5 + y) = -6 \cdot 5 + (-6 \cdot y)$$

4) Identity Prop

$$a + 0 = a$$

$$7 + 0 = 7$$

$$a \cdot 1 = a$$

$$-100 \cdot 1 = -100$$

$$-3x + 0 = -3x$$

$$4xy^2 \cdot 1 = 4xy^2$$

5) Inverse Prop.

$$a + (-a) = 0$$

$$23 + (-23) = 0$$

$$a \cdot \frac{1}{a} = 1 ; a \neq 0$$

$$4 \cdot \frac{1}{4} = 1$$

Simplify

$$5(x + 2) - 10$$

$$= 5x + 10 - 10$$

Distribute

$$= 5x + 0 = 5x$$

Inverse
Identity

$$-8x + 8x = 0$$

$$-\frac{3}{5} \cdot -\frac{5}{3} = 1$$

Simplify

$$2\left(\frac{1}{2}x - 1\right) + 2$$

$$= 2\left(\frac{1}{2}x\right) - 2 \cdot 1 + 2$$

Distribution

$$= (2 \cdot \frac{1}{2})x - 2 \cdot 1 + 2$$

Associative

$$= 1x - 2 \cdot 1 + 2$$

Inverse

$$= x - 2 + 2$$

Identity

$$= x + 0$$

Inverse
Identity

$$= \boxed{x}$$

Simplify

$$4(2x + 5) - 5(x + 4)$$

$$= 4(2x) + 4(5) - 5x - 5(4) \quad \text{Distribution}$$

$$= (4 \cdot 2)x + 20 - 5x - 20 \quad \text{Associative}$$

$$= 8x + 20 - 5x - 20$$

$$= 8x - 5x + 20 - 20 \quad \text{Commutative}$$

$$= 3x + 0$$

$$= \boxed{3x}$$

Inverse

Identity

Simplify and name the properties:

$$\frac{3}{5} \left(\frac{5}{3}x + 1 \right) - \frac{3}{5}$$

$$= \frac{3}{5} \left(\frac{5}{3}x \right) + \frac{3}{5} \cdot 1 - \frac{3}{5} \quad \text{Distribution}$$

$$= \left(\frac{3}{5} \cdot \frac{5}{3} \right) x + \frac{3}{5} \cdot 1 - \frac{3}{5} \quad \text{Associative}$$

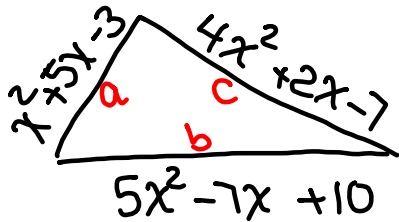
$$= 1 \cdot x + \frac{3}{5} \cdot 1 - \frac{3}{5} \quad \text{Inverse}$$

$$= x + \frac{3}{5} - \frac{3}{5} = x + 0$$

$$= x$$

Identity
Inverse
Identity

Find an expression in simplest form for the perimeter of $P = a + b + c$



$$P = x^2 + 5x - 3 + 4x^2 + 2x - 7 + 5x^2 - 7x + 10$$

$$P = \underbrace{x^2 + 4x^2 + 5x^2}_{\text{Commutative}} + \underbrace{5x + 2x - 7x}_{\text{Inverse}} - \underbrace{3 - 7 + 10}_{\text{Identity}}$$

$$= 10x^2 + 0 + 0$$

$$= 10x^2$$

Translate, then Simplify

4 times the sum of -2 and 3 times some number increased by 8.

$$4(-2 + 3x) + 8$$

$$= 4(-2) + 4(3x) + 8$$

$$= -8 + 4(3x) + 8$$

$$= 4(3x) - 8 + 8$$

$$= (4 \cdot 3)x - 8 + 8$$

$$\rightarrow = 12x + 0$$

$$= \boxed{12x}$$

Agenda For tomorrow:

- 1) Collect SG 1 at 9:00 AM
- 2) Class QZ 2 at 9:00 AM
- 3) Start on ch. 2

Start working on ch. 1 of
word Problems.